



# Parameterizing large-scale circulations based on the weak temperature gradient approximation

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# Overview



- Weak temperature gradient parameterization: how it works
- Circulations in a homogeneous environment
- Circulations in an inhomogeneous environment
- Transitional cases and parameterization testing





# Weak temperature gradient parameterization: how it works



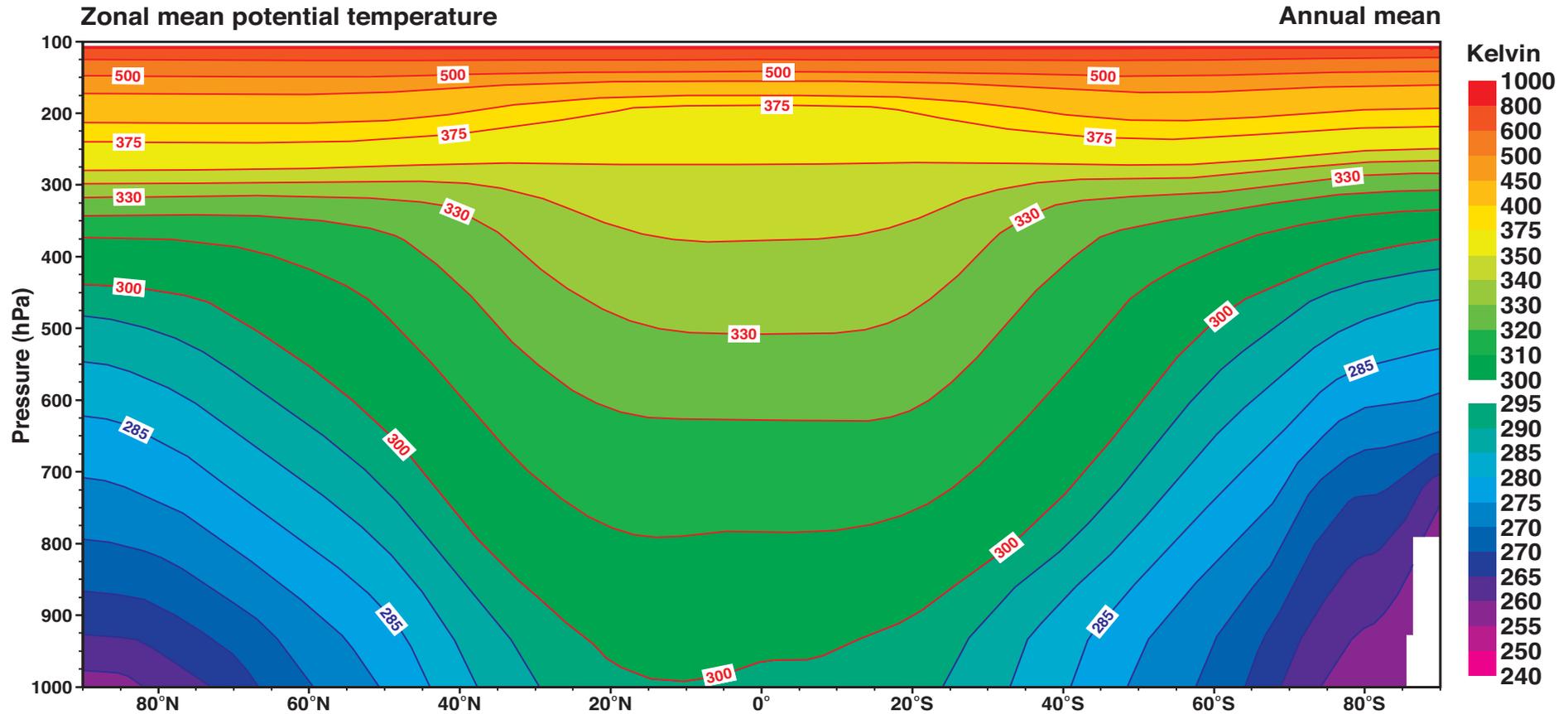
# Modelling approaches



- Large-domain and high-resolution simulations
- GCM: simulate the large-scale circulation but parameterize the convection
- CRM: impose the large-scale circulation and simulate the convection
- SCM: impose the large-scale circulation and test parameterization of the convection (too easy?)
- Today: parameterize the large-scale circulation and simulate the convection
- Also: parameterize the large-scale circulation and parameterize the convection



# Weak temperature gradients



- Little variation in free troposphere over the tropics

# Basic ideas



- Gravity waves are effective in redistributing density anomalies so as to maintain near uniform density on isobaric surfaces
- This leads to large-scale circulations which act to balance local anomalies of heating so as to produce quasi-uniform potential temperature
- The boundary layer is different because conditions there are tied to the local underlying surface temperature



# Diagnosing circulations

$$\frac{\partial \theta}{\partial t} + \mathbf{v} \nabla_h \theta + w \frac{\partial \theta}{\partial z} = S \quad (1)$$

On the large scale, simplify to

$$\bar{w} \frac{\partial \bar{\theta}}{\partial z} \approx \bar{S} = Q_R + Q_c \quad (2)$$

- Based on  $\bar{S}$ , can evaluate the  $\bar{w}$  required for the WTG balance
- Can enforce Eq. 2 by resetting  $\theta(t, z) = \theta(z)$ , and allow the diagnosed  $\bar{w}$  to produce a source/sink term in moisture equation (Sobel and Bretherton, 2000)
- $\theta(z)$  typically taken from RCE

# Relaxation form

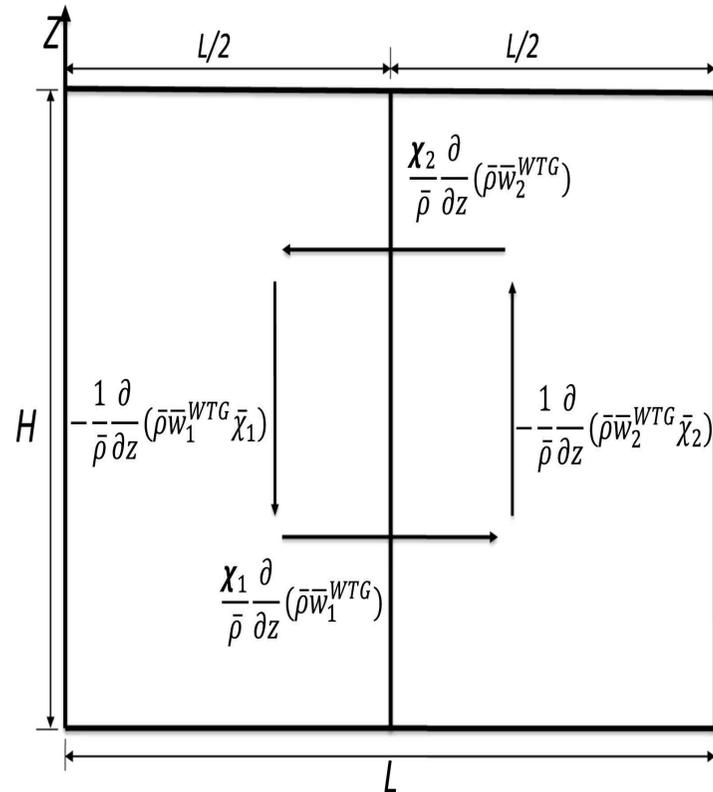
A weaker version envisages gravity waves reducing temperature difference over a finite timescale  $\tau$ ,

$$\bar{w} \frac{\partial \bar{\theta}}{\partial z} = \frac{1}{\tau} (\bar{\theta} - \bar{\theta}_{\text{ref}}) \quad (3)$$

(Raymond and Zeng, 2005)

- $\tau$  is of order a few hours, corresponding to lengthscales of order 1000 km for gravity waves of order  $50 \text{ ms}^{-1}$
- Reference state typically taken from RCE
- The RCE surroundings do not vary in response to the WTG-derived circulation

# Generalize to two regions



- Reference state imagines open system with coupling to infinite reservoir
- Consider two regions with a diagnosed circulation affecting both
- Allows study of influence of remote changes on local convection

# Generalization to two regions

$$\bar{w}_2 \frac{\partial}{\partial z} \bar{\theta}_2 - \bar{w}_1 \frac{\partial}{\partial z} \bar{\theta}_1 = \frac{1}{\tau} (\bar{\theta}_2 - \bar{\theta}_1) \quad (4)$$

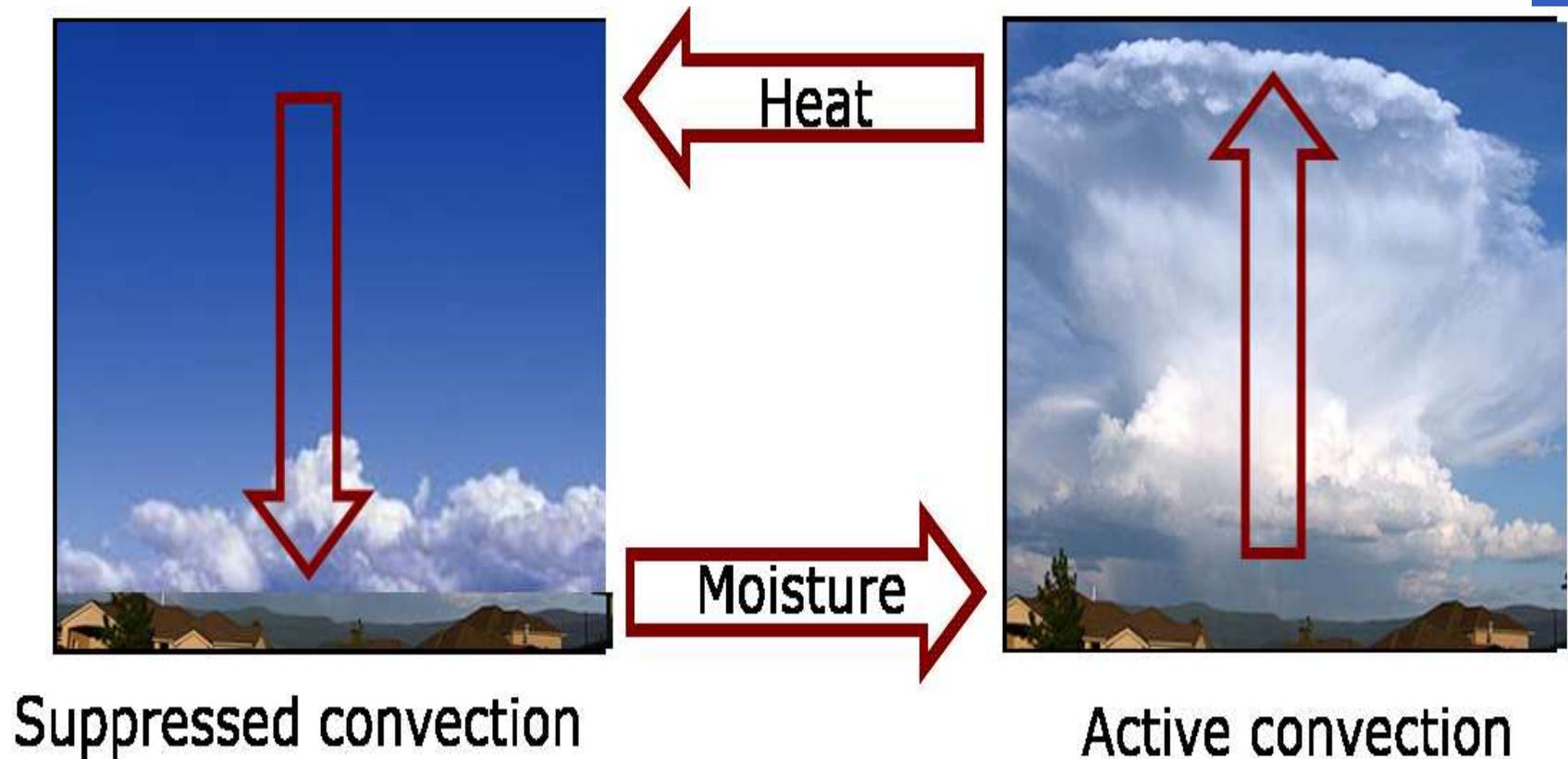
For continuity

$$(1 - \varepsilon) \bar{w}_1 + \varepsilon \bar{w}_2 = 0 \quad (5)$$

leading to

$$\bar{w}_1 = \frac{1}{\tau} \left[ \frac{\bar{\theta}_1 - \bar{\theta}_2}{\frac{\partial \bar{\theta}_1}{\partial z} + \left( \frac{1 - \varepsilon}{\varepsilon} \right) \frac{\partial \bar{\theta}_2}{\partial z}} \right] \quad (6)$$

Recovers reservoir formula for relative area  $\varepsilon \rightarrow 0$  or  $1$ .



- We also associate a horizontal WTG velocity with  $\bar{w}_{wtg}$  in order to close the circulation
- This gives a closed two-region approach constrained by energy and moisture conservation

# Treatment of boundary layer



- Boundary layer conditions tied to the local SST
- Treatment is to calculate  $w_{\text{WTG}}$  for heights above some nominal BL top, say 1.5km, and linearly interpolate between  $w_{\text{WTG}}(z_{\text{BL}})$  and  $w_{\text{WTG}}(z = 0) = 0$
- We will return to this...

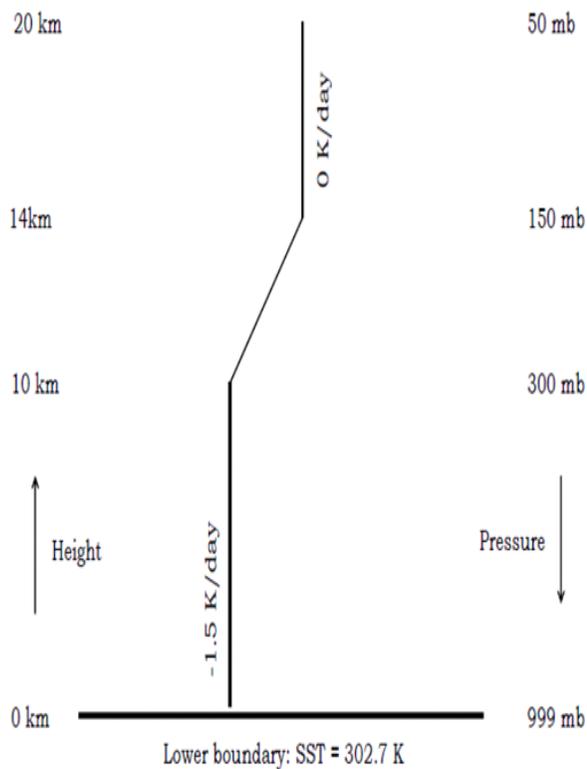




# Circulations in a homogeneous environment



# Models used



- Run to equilibrium with prescribed radiative cooling
- Typically for 40 days, with first 20 discarded as spin-up
- Using LEM, 2D with  $\Delta x = 500$  m
- Also use some GASS WTG intercomparison results for reference-state cases

# Reference state, same SST



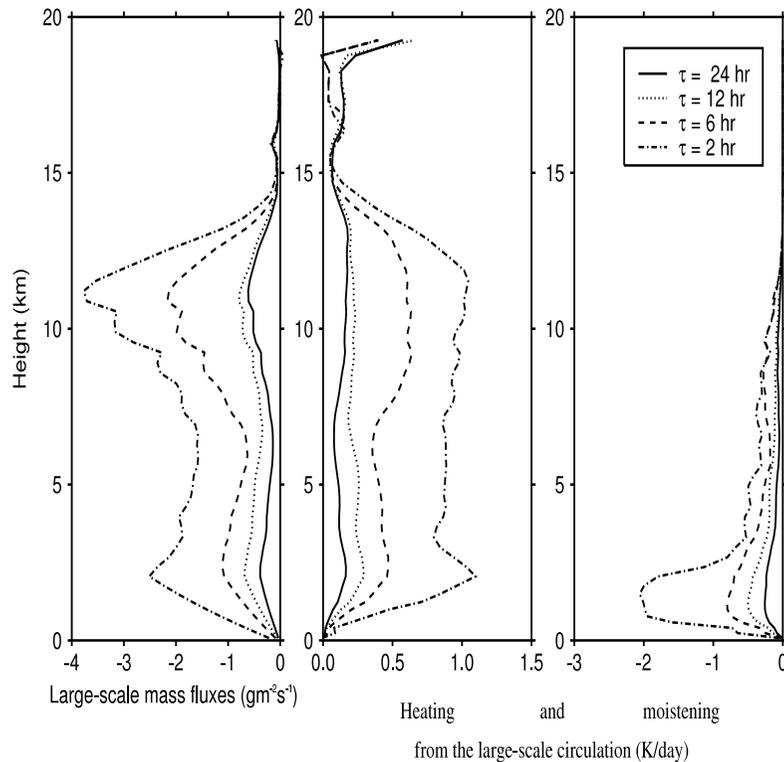
- Generate RCE reference state
- Make a WTG coupling to this state with simulated region initialized to the RCE state
- Use identical forcing and surface conditions to the RCE configuration
- What happens?



# Reference state, same SST



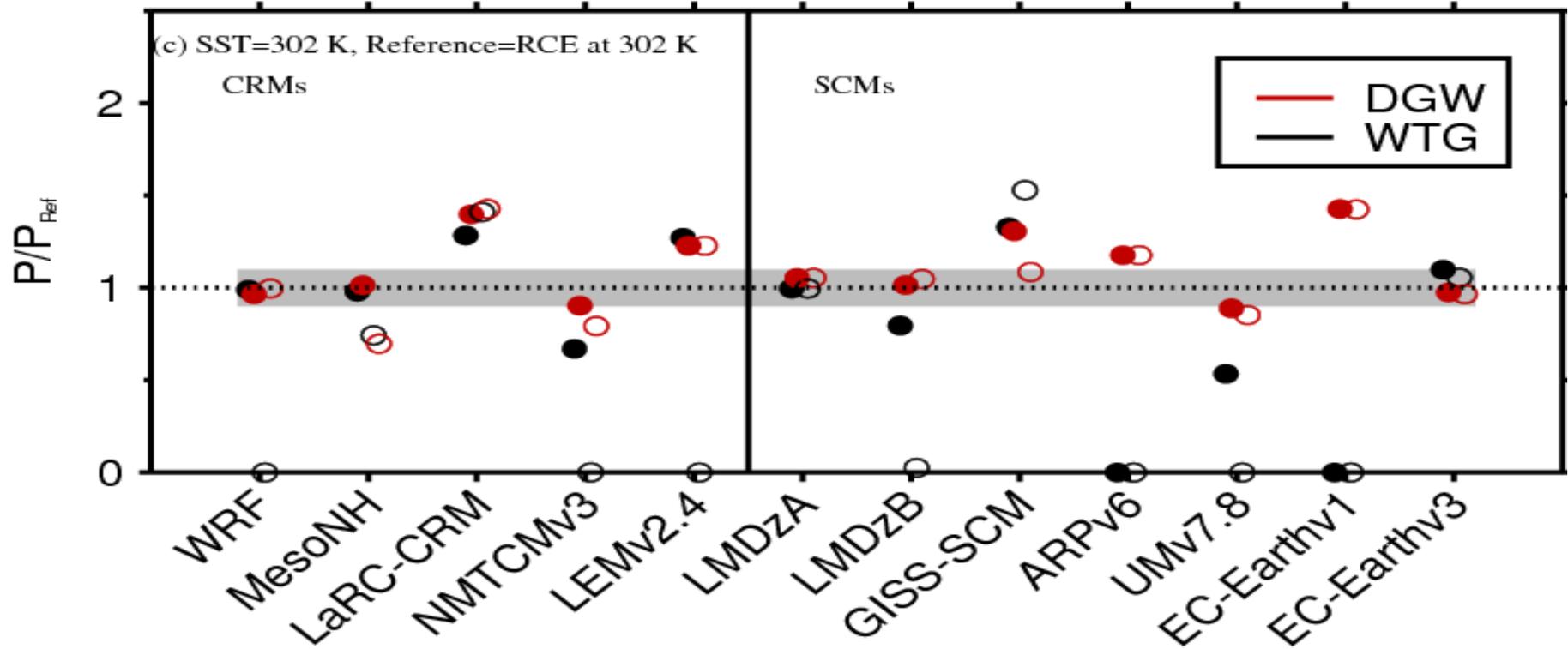
- **Descent in simulated region** with associated heating and drying tendencies



| mm/d           | Rain | Evap |
|----------------|------|------|
| RCE            | 4.77 | 4.80 |
| $\tau = 120$ h | 4.70 | 4.74 |
| $\tau = 24$ h  | 4.40 | 4.77 |
| $\tau = 12$ h  | 4.03 | 4.78 |
| $\tau = 6$ h   | 3.43 | 4.64 |
| $\tau = 2$ h   | 1.99 | 4.47 |



# Other models



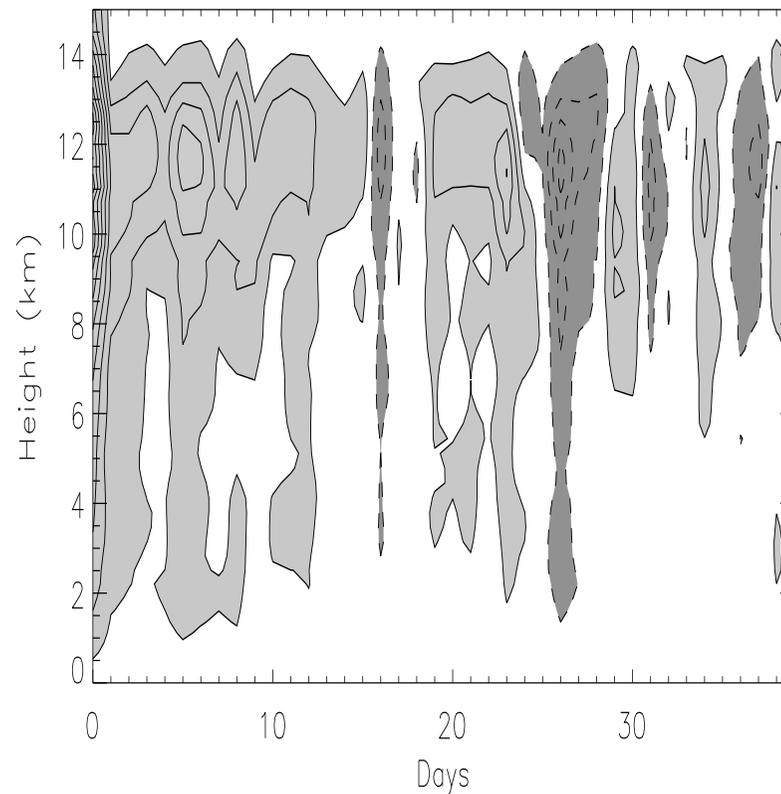
- Some develop large-scale circulations within a homogeneous environment
- Some support multiple equilibria



# Two region configuration



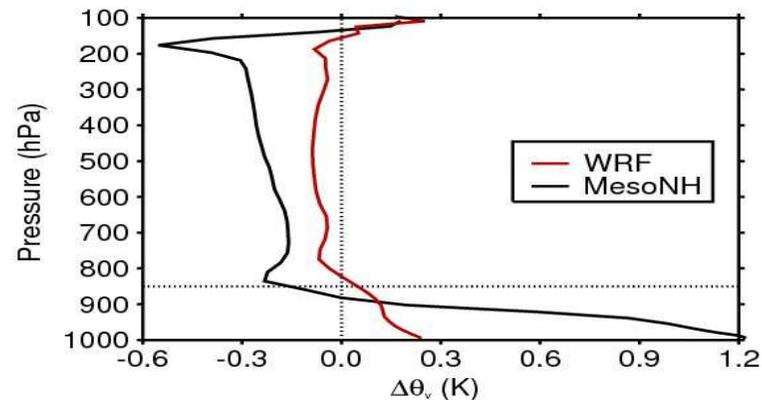
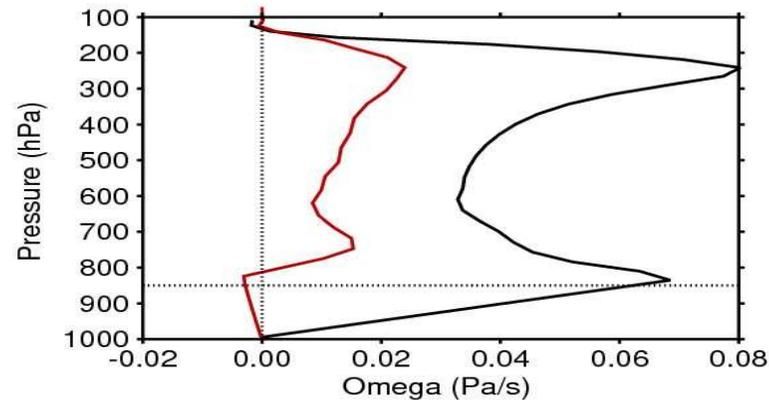
- Produces no time-mean WTG circulation irrespective of  $\varepsilon$
- Adjustment to equilibrium much slower for small  $\varepsilon$
- **But** note small  $\varepsilon$  qualitatively different from reference configuration



# Role of Boundary Layer Top



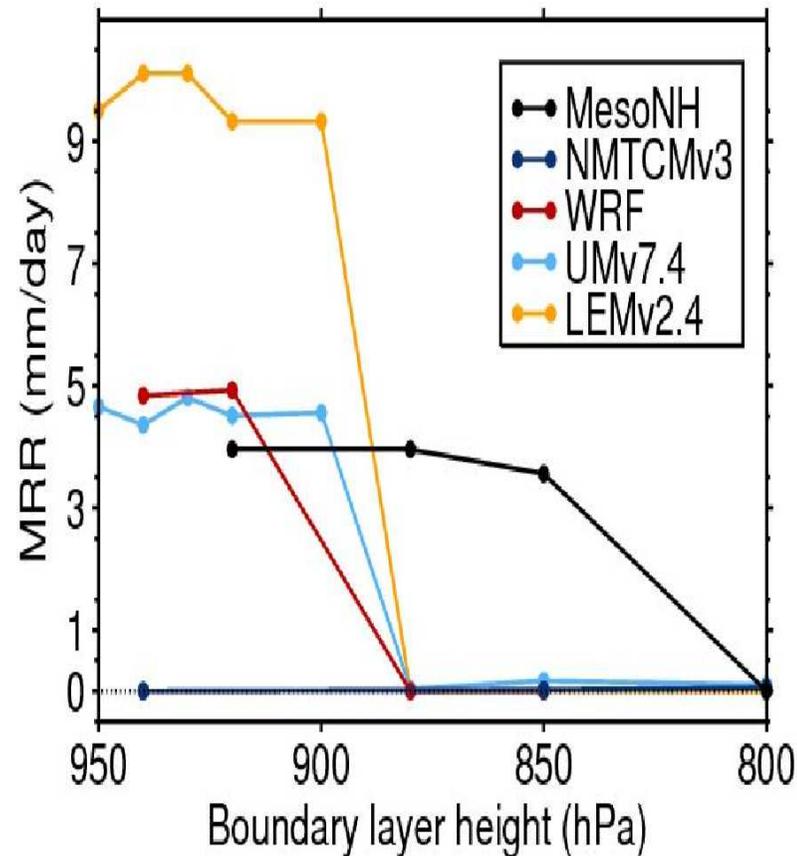
- Consider  $w_{\text{WTG}}$  profiles in cases of dry equilibria
- Change of sign can occur close to BL top
- Sign may differ from that which would have been expected without the linear interpolation prescription



# Varying the Boundary Layer Top



- Critical BL depth to get the dry state: equilibrium state can be made precipitating by setting a lower depth (but still above mixed layer)
- Some dependence of multiple states on SST (more likely if higher) and  $\tau$  (more likely if shorter)





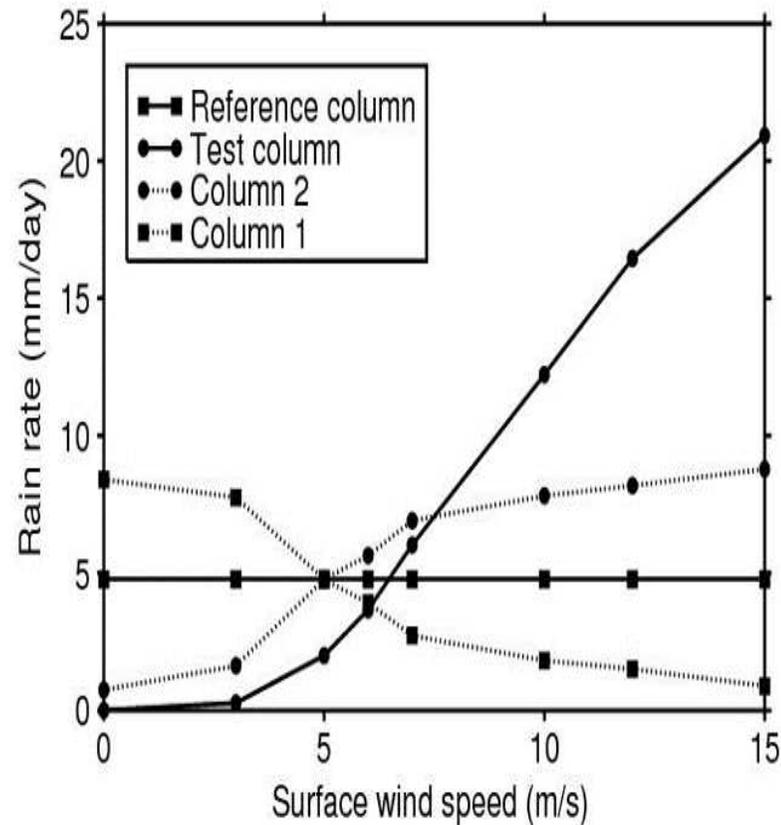
# Circulations in an inhomogeneous environment



# Precipitation variations



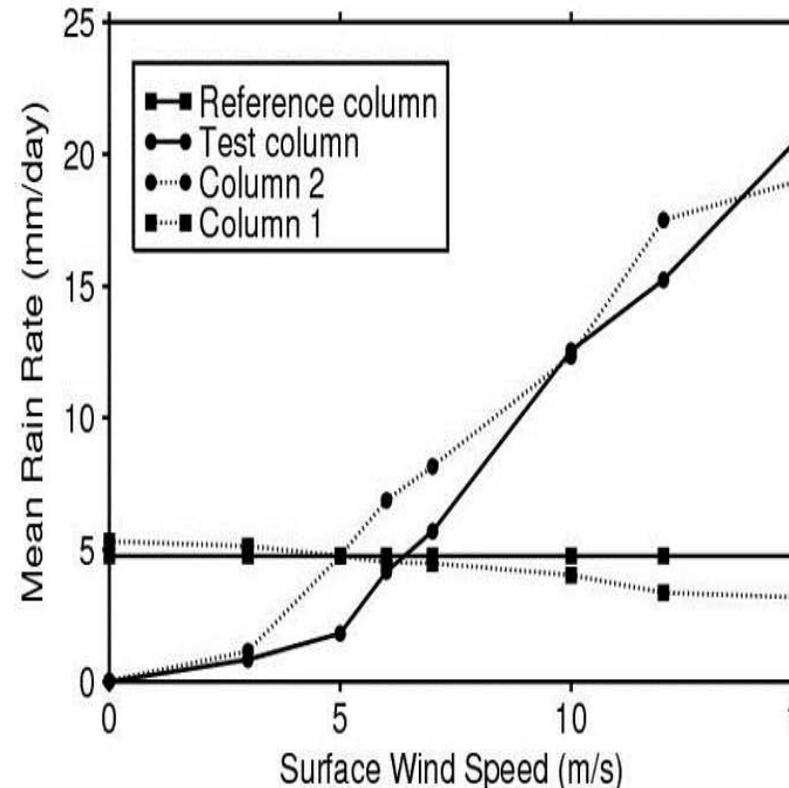
- Vary surface wind speed with  $\tau = 2$  h for reference column case and for  $\varepsilon = 0.5$
- Two region case less sensitive due to constraints from closed budgets



# Precip variations for small $\varepsilon$

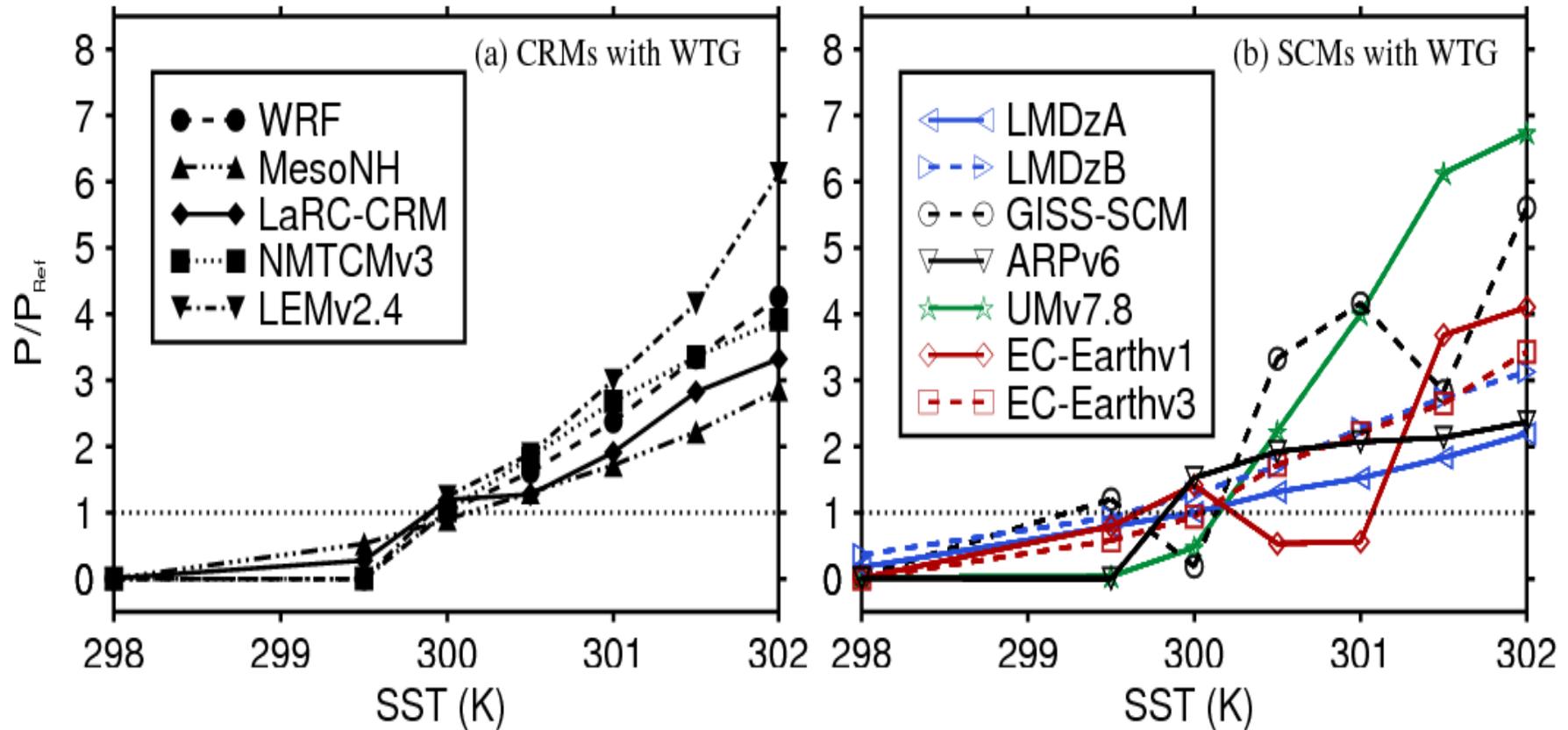


- Comparison against  $\varepsilon = 0.1$  and  $\tau = 4$  h
- Similar to reference approach at  $\tau = 2$  h for large changes in surface conditions
- But differences remain for small changes



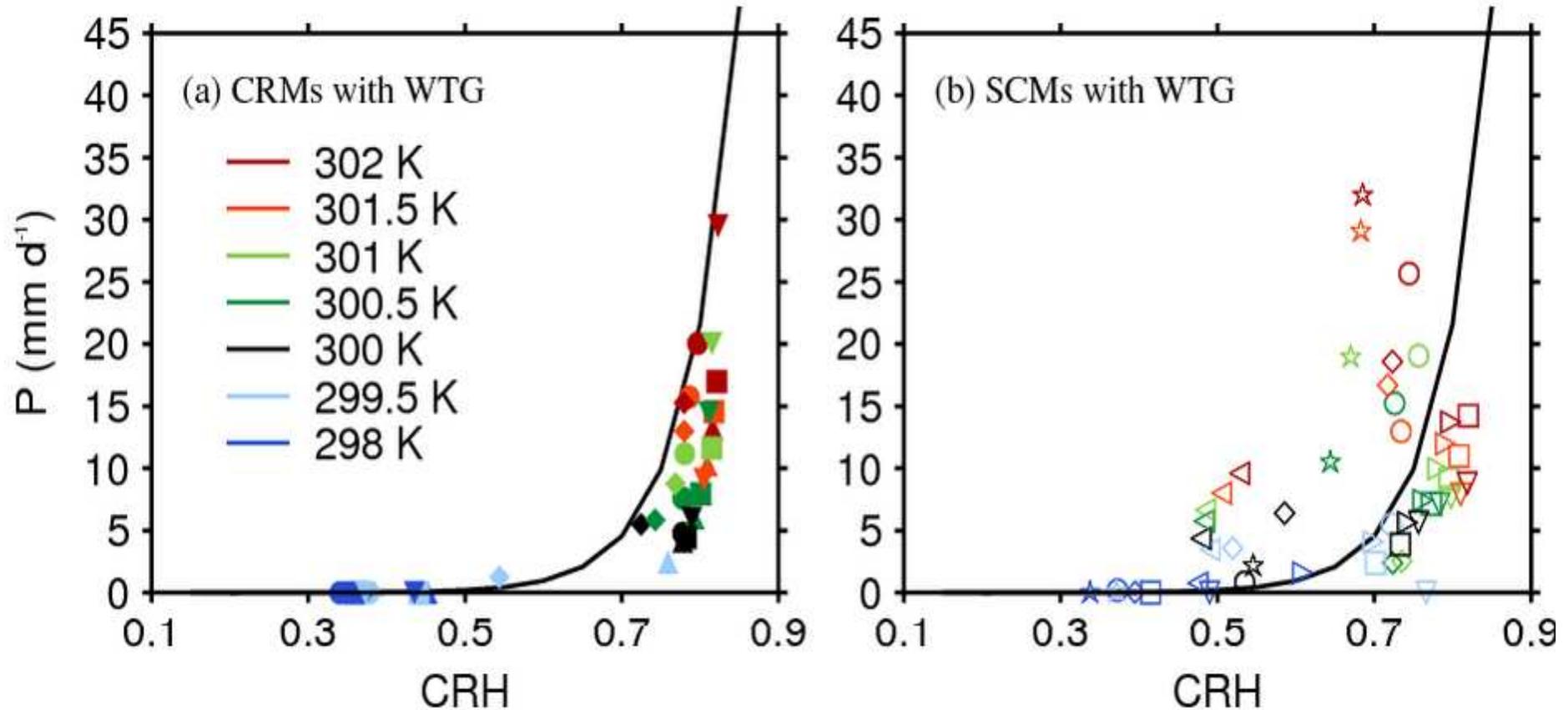
# Comparison of models

Varying SST in reference-state approach



# Precip and column relative humidity

Comparison with observational fit from satellite data over tropical oceans



# Transitional cases and parameterization testing



# Transition, suppressed $\rightarrow$ active



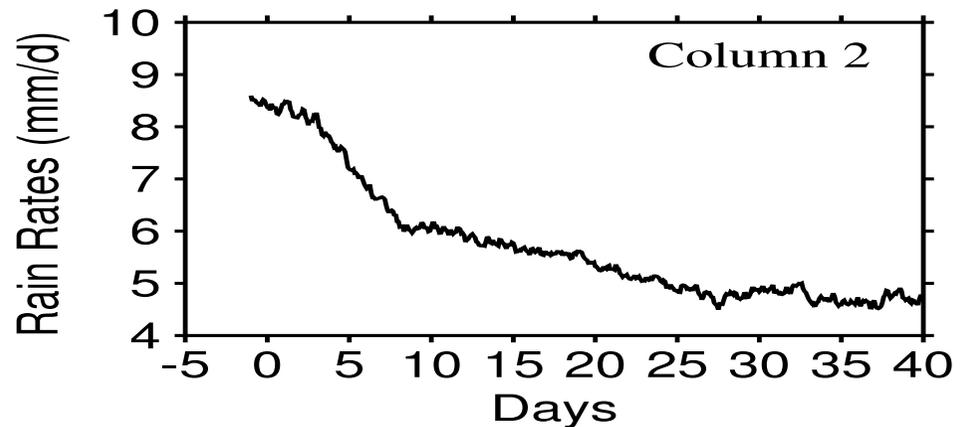
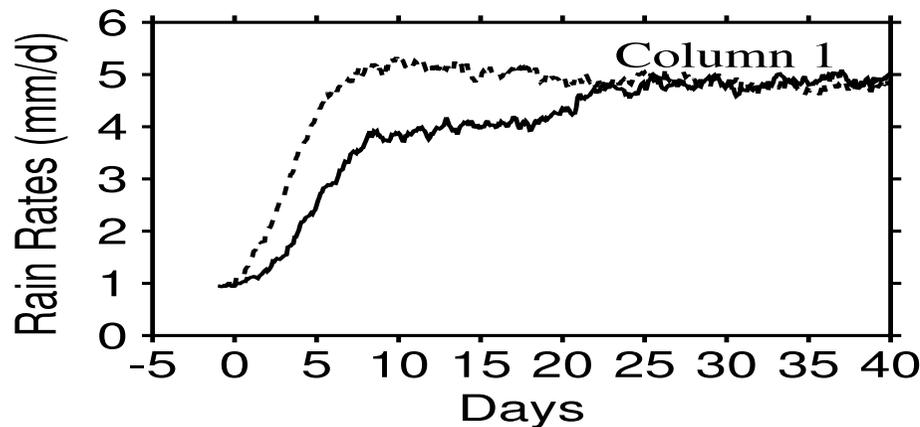
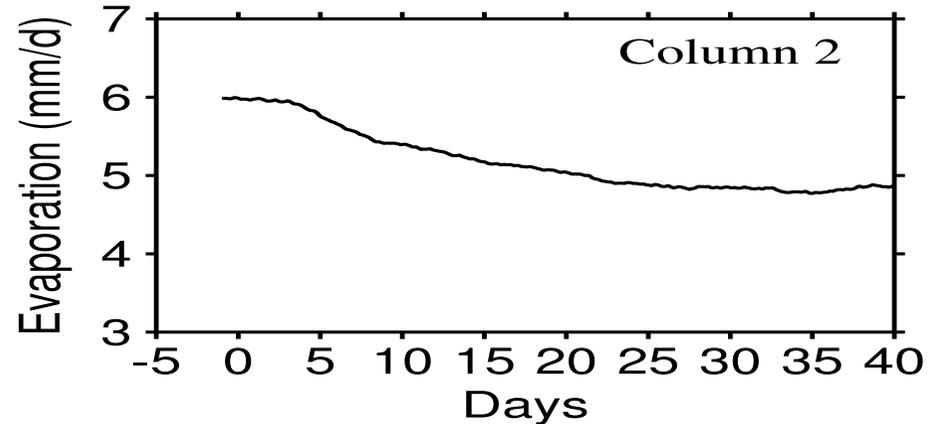
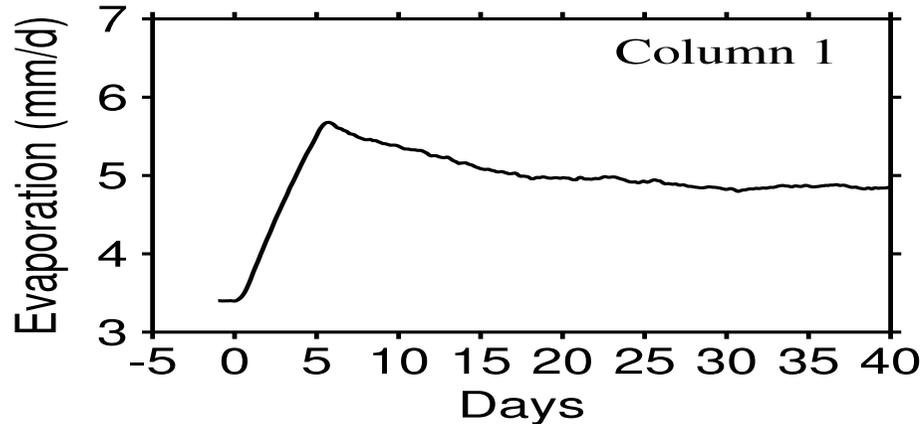
- Start from equilibrium state of two-region configuration with SST difference of 2K
- Rain rates are 0.98 and 8.47 mm/d in cold and warm regions
- Now transition to state of equal SST, no circulation, by
  1. local transition: increase cold SST by 2K
  2. remote transition: decrease warm SST by 2K
  3. mixed transition: increase cold and decrease warm SST by 1K



# Local transition



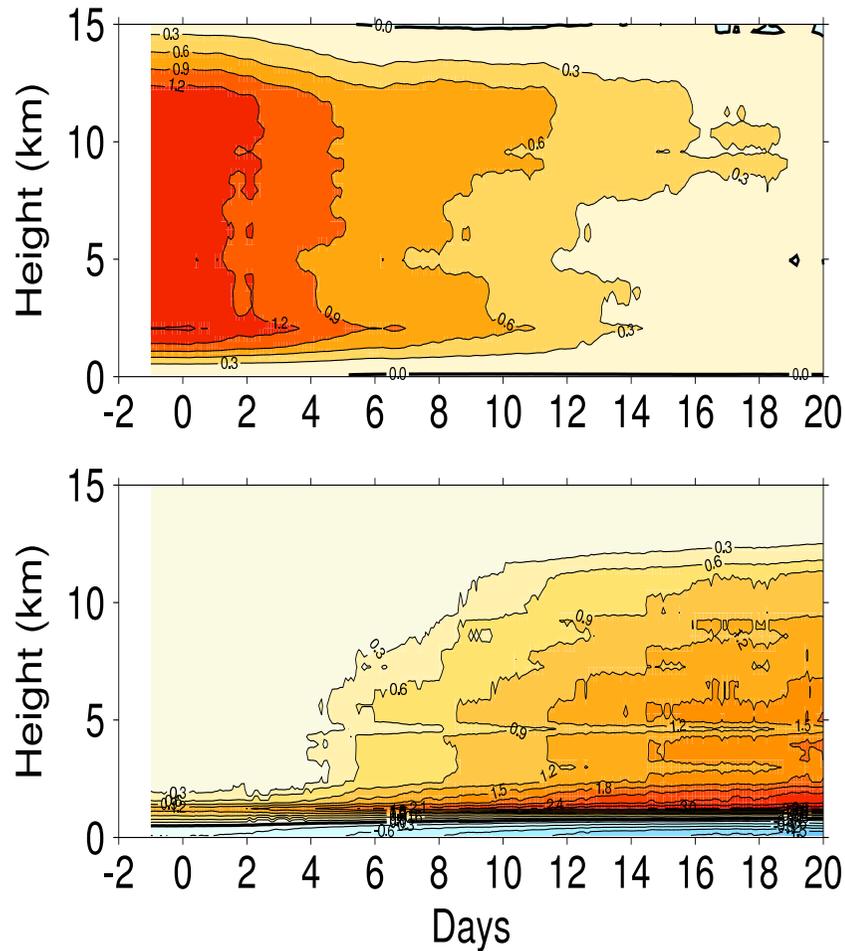
The need to remove the WTG circulation slows the transition



Dashed line, set circulation to zero at transition time



# Remote transition



- Reduce evaporation in active region
- Leads to reduced convection there
- Reduces circulation
- Ultimately enough to allow convection in suppressed region

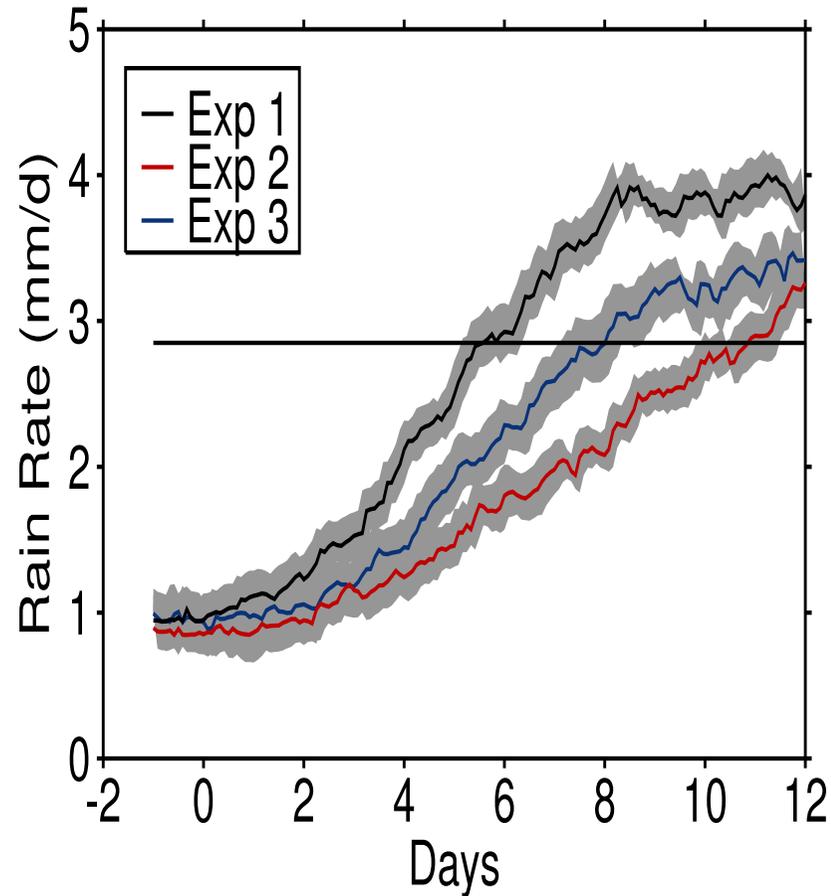


# Transition times



| Type   | Time      |
|--------|-----------|
| Local  | 5.4 days  |
| Remote | 10.9 days |
| Mixed  | 8.7 days  |

Transition time: that required for rain rate to increase by half the amount needed to reach new equilibrium



# Comparison with SCM



| Type   | CRM  | SCM |
|--------|------|-----|
| Local  | 5.4  | 3.9 |
| Remote | 10.9 | 5.9 |
| Mixed  | 8.7  | 4.8 |

- Repeat same transition experiments with the UM SCM (v7.8)
- All of the transitions are faster
- In the CRM, heating and moistening effects of large-scale circulation are about equally divided
- In the SCM, heating effects more important than moistening



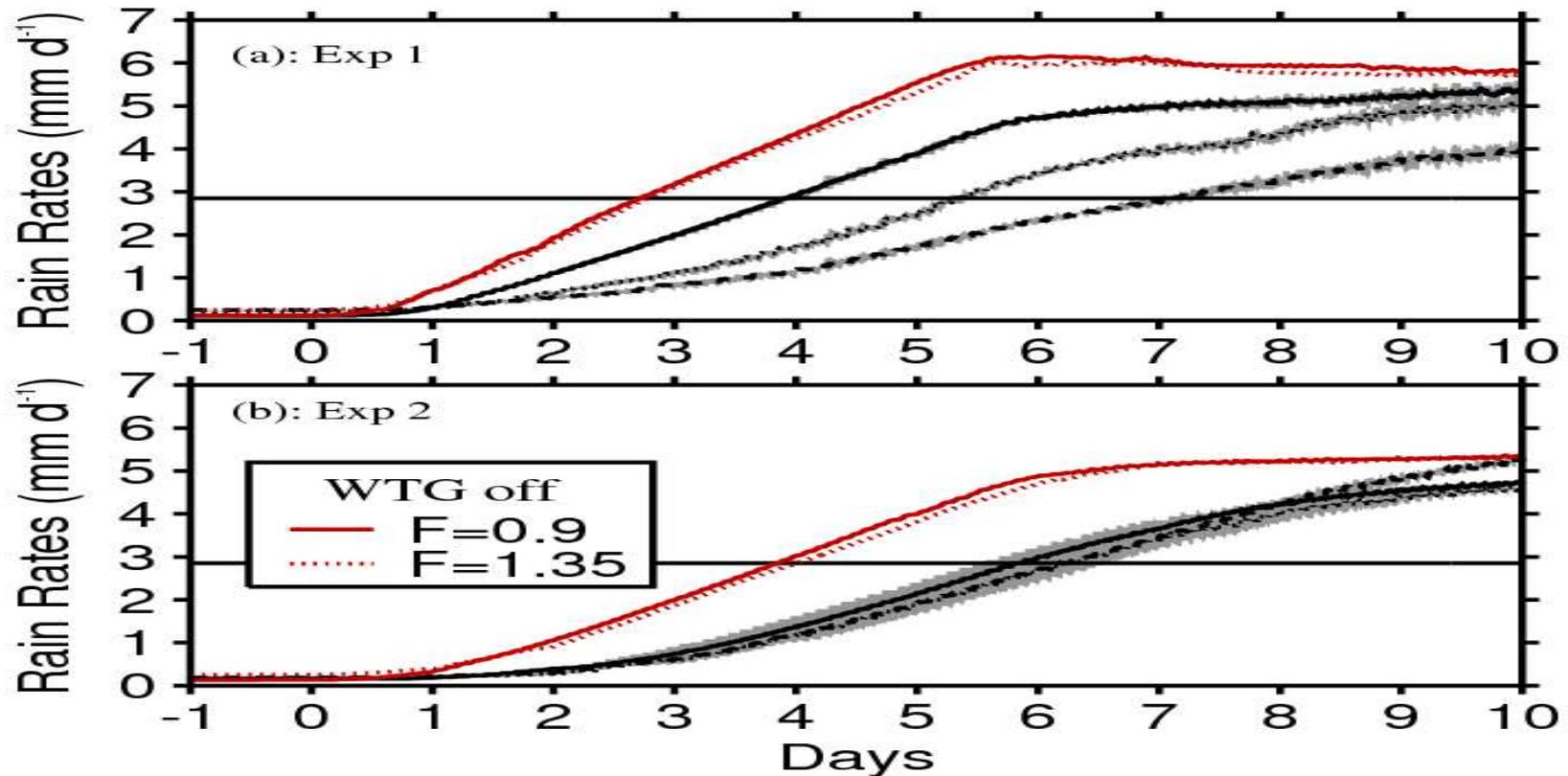
# Simple parameterization tests



- Vary closure timescale of UM convection parameterization
  - very little effect: only alters high-frequency variability
- Vary entrainment and detrainment rates of UM convection parameterization
  - This is a **key source of uncertainty in GCMs** for both mean state and some modes of variability
  - We increase the entrainment and detrainment rates by 25% and 50%

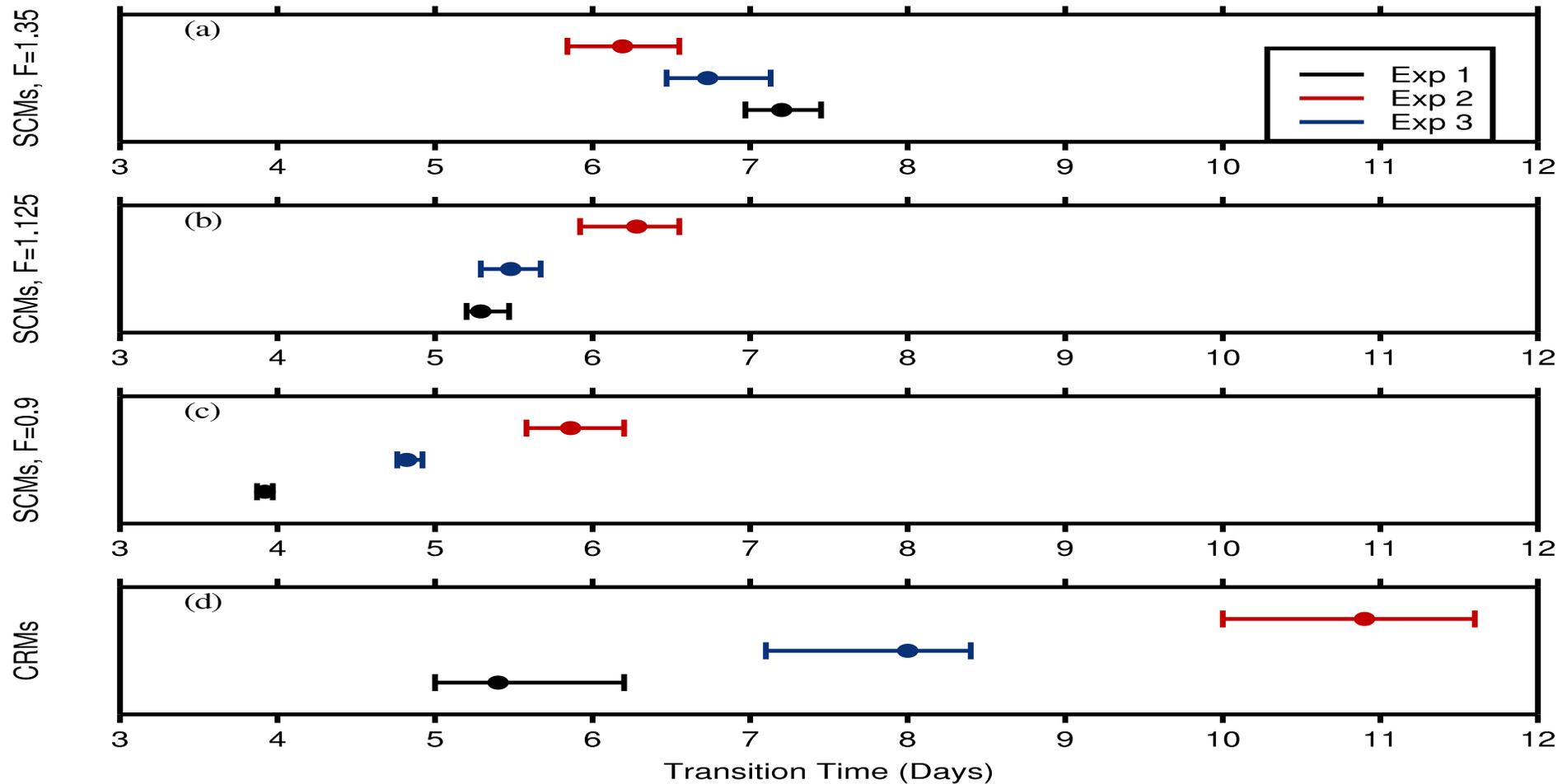


# Changes to entrainment



Feedback effects of entrainment rate on large-scale circulation do matter, rather than any more direct effect

# Effects on Transition Times



A non-trivial test of parameterization interactions with large-scale circulation

# Summary I



- WTG approach allows coupling between convection and large-scale tropical circulations
- Normally coupling is to a reference RCE state and system is open
- This can produce ascent/descent/no circulation for uniform SST depending on the convection model
  - Caution: this does not happen in a closed two-region approach for any  $\varepsilon$
- And can have multiple equilibrium with a non-precipitating state
  - Caution: this is very sensitive to the rather arbitrary treatment of the boundary layer circulation



# Summary II



- For distinct surface conditions, can produce good precip vs  $w_{LS}$  and precip vs CRH relationships
- CRH relation under WTG may provide a good test for SCM parameterizations
- The two region approach allows simulation of new idealized problems: e.g., effects of remote changes on suppressed → active transitions
- Transitions under WTG may provide a difficult test for SCM parameterizations



# References

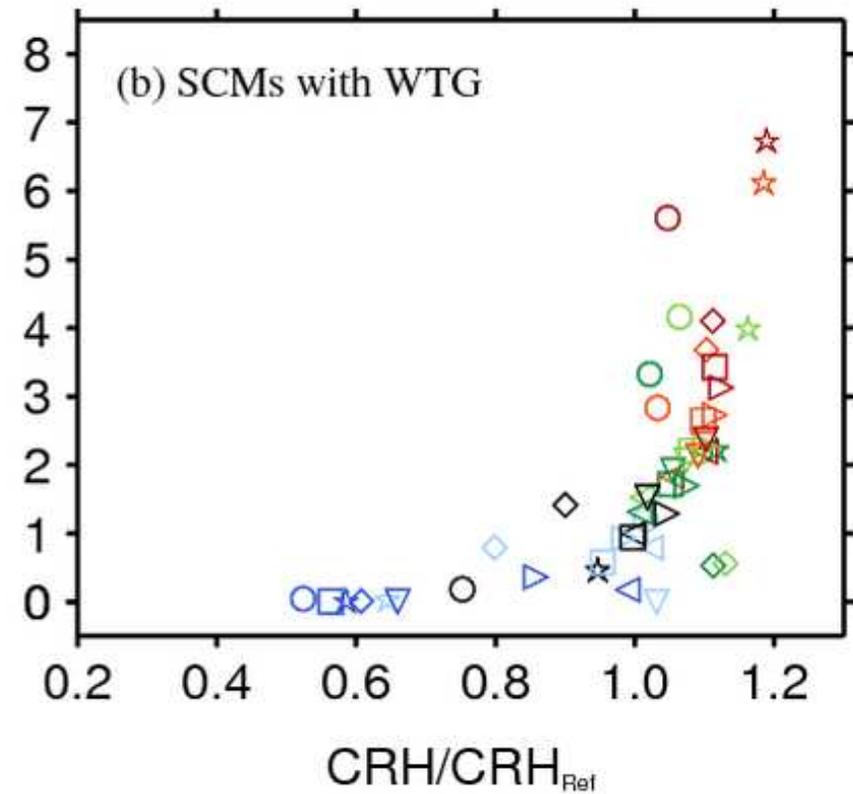
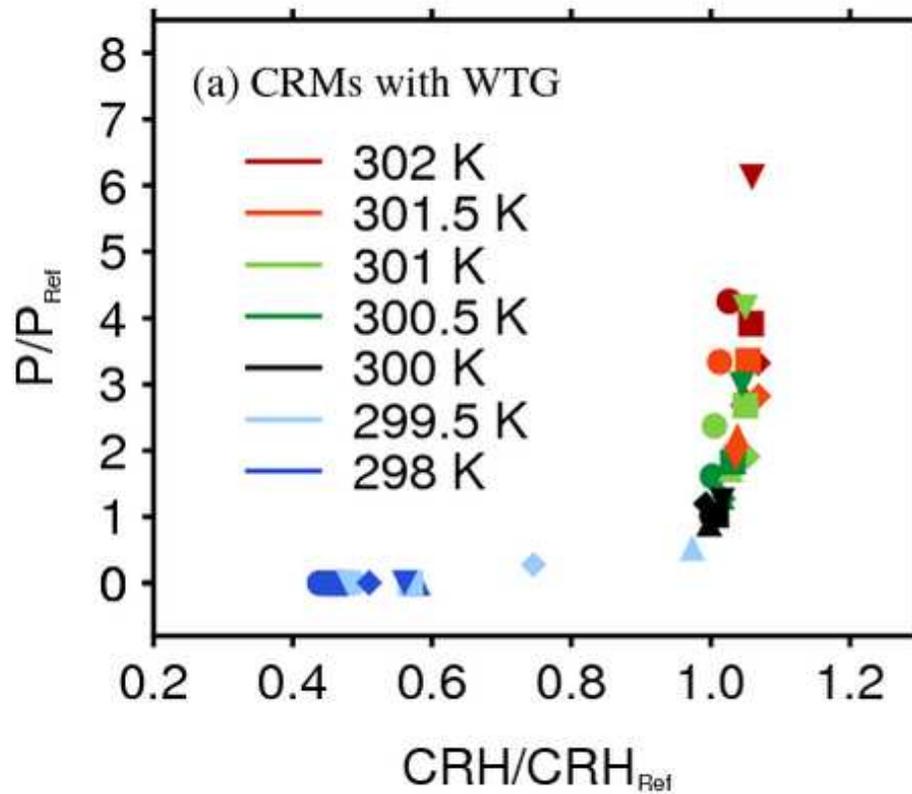


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# Precip and column relative humidity

Some collapse if scaled by reference RCE values

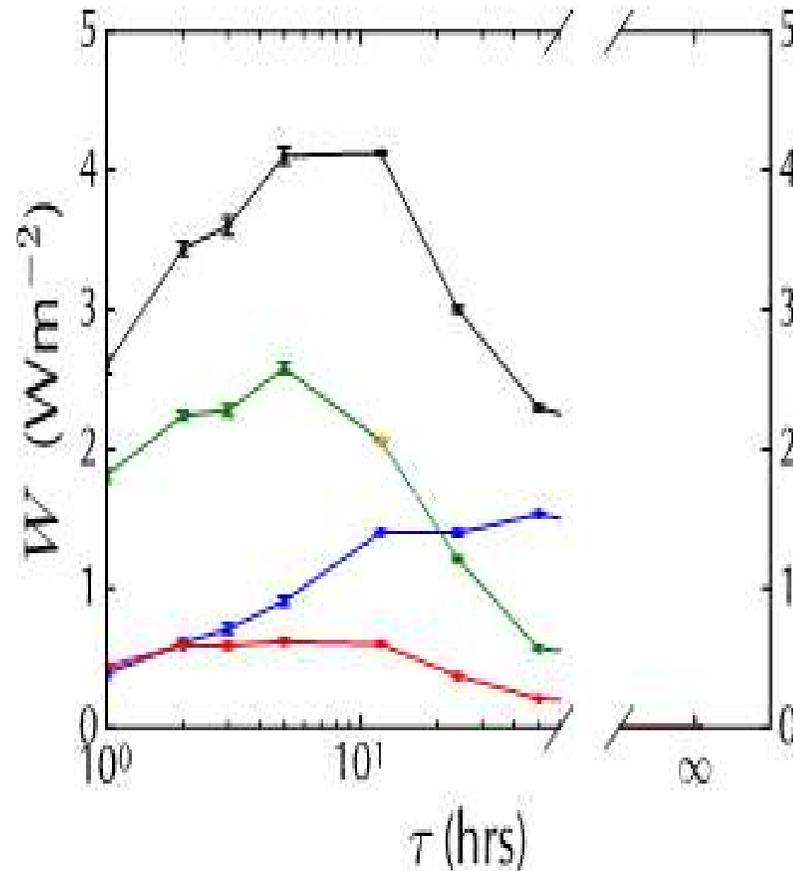


# Thermodynamic Analysis

$$\oint T dS \approx \oint B dz$$

$$+ g \oint r_T dz$$

$$- \sum_{w=v,l,i} \oint G_w dr_w$$



With Kamieniecki, Ambaum